Homework 9 (due 6/10)

- 1. Exercise 2.4.3.
- 2. Exercise 2.4.13(a), (b).
- 3. Let T be a torus parametrized by

$$\mathbf{x}(u,v) = ((a+b\cos u)\cos v, (a+b\cos u)\sin v, b\sin u), \ a > b.$$

Prove that

- (a) If a geodesic is tangent to the parallel $u = \frac{\pi}{2}$, then it is entirely contained in the region of T given by $-\frac{\pi}{2} \le u \le \frac{\pi}{2}$.
- (b) A geodesic that intersects the parallel u = 0 under an angle $\phi (0 < \phi < \frac{\pi}{2})$ also intersects the parallel $u = \pi$ if $\cos \phi < \frac{a-b}{a+b}$.

Hint: Use Clairaut's relation. You might also need to use the result of Exercise 2.4.6.