

7. Let  $(X, \mathfrak{B})$  be a measurable space and on it,  $\nu$  is a finite measure and  $\mu$  a  $\sigma$ -finite measure, show the following are equivalent:
- (a)  $\nu \ll \mu$  and
  - (b) If the sequence  $E_n \subseteq \mathfrak{B}$  has the property that  $\lim_{n \rightarrow \infty} \mu(E_n) = 0$ , then  $\lim_{n \rightarrow \infty} \nu(E_n) = 0$ .
8. (a) Show: The normed vector space  $L^p(\mu)$  is a Banach space.
- (b) Let  $\phi$  be a continuous linear map from  $\mathbb{R}^n$  into a normed vector space  $F$ . Find the sup norm of  $\phi$ .