# **Probability Prelim**

σ-Algebra (σ-field) Construction of Probability Space Dynkin's Theorem (Monotone Class Theorem)

## Independence

Borel-Cantelli Lemma Borel zero-one law Kolmogorov's zero-one law

#### Expectation

Transformation Theorem Fubini Theorem

## Inequalities

Hölder's Inequality Minkowski Inequality Jensen's Inequality

# **Convergence Concept**

Convergence almost surely Convergence in probability Convergence in L^p Convergence in distribution Uniform Integrability Portmanteau Theorem Tightness and Pohorov's Theorem Selection Theorem Characteristic Functions

# **Convergence Theorem**

Central Limit Theorem Weak Law of Large Numbers Strong Law of Large Numbers Kolmogorov Three Series Theorem

#### Martingale

Conditional Probability and Expectation Doob's Decomposition Stopping Times and Optional Sampling Theorem Doob's Submartingale Convergence Theorem

Textbook : A Probability Path by Resnick