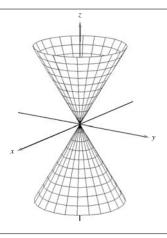
468 **CHAPTER 7** Functions of Several Variables



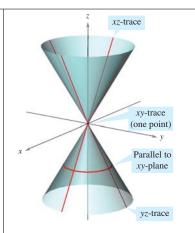
Elliptic Cone

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 0$$

Trace Plane

Ellipse Parallel to xy-plane
Hyperbola Parallel to xz-plane
Hyperbola Parallel to yz-plane

The axis of the cone corresponds to the variable whose coefficient is negative. The traces in the coordinate planes parallel to this axis are intersecting lines.



X y

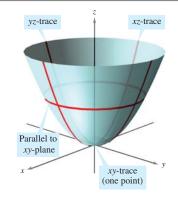
Elliptic Paraboloid

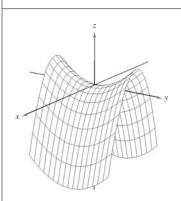
$$z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$$

Trace Plane

Ellipse Parallel to *xy*-plane
Parabola Parallel to *xz*-plane
Parabola Parallel to *yz*-plane

The axis of the paraboloid corresponds to the variable raised to the first power.





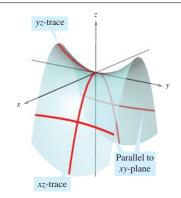
Hyperbolic Paraboloid

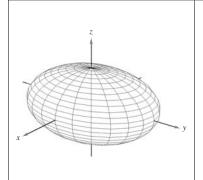
$$z = \frac{y^2}{b^2} - \frac{x^2}{a^2}$$

Trace Plane

Hyperbola Parallel to xy-plane
Parabola Parallel to xz-plane
Parabola Parallel to yz-plane

The axis of the paraboloid corresponds to the variable raised to the first power.





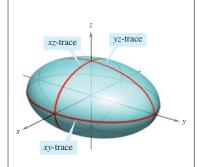
Ellipsoid

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$

Trace Plane

Ellipse Parallel to xy-plane
Ellipse Parallel to xz-plane
Ellipse Parallel to yz-plane

The surface is a sphere if the coefficients a, b, and c are equal and nonzero.



x y

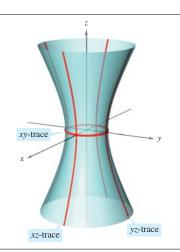
Hyperboloid of One Sheet

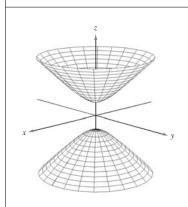
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 1$$

Trace Plane

Ellipse Parallel to xy-plane Hyperbola Parallel to xz-plane Hyperbola Parallel to yz-plane

The axis of the hyperboloid corresponds to the variable whose coefficient is negative.





Hyperboloid of Two Sheets

$$\frac{z^2}{c^2} - \frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

Trace Plane

Ellipse Parallel to xy-plane Hyperbola Parallel to xz-plane Hyperbola Parallel to yz-plane

The axis of the hyperboloid corresponds to the variable whose coefficient is positive. There is no trace in the coordinate plane perpendicular to this axis.

