

1. Find $\frac{\partial w}{\partial \theta}$ if $w = e^x \sin y$ and $x = r \cos \theta, y = r \sin \theta$
2. If $x^3 + y^3 + z^3 - 5x^2y^2z^2 = 5$ find $\frac{\partial z}{\partial y}$
3. Let $w = xyz, x = \sin 2t, y = \cos 2t, z = e^{-t}$. Find $\frac{dw}{dt}$.
4. Find relative maximum, minimum and saddle points of

$$f(x, y) = x^3 - 3xy + y^3.$$

5. Use polar coordinate to prove: $\lim_{(x,y) \rightarrow (0,0)} \frac{x^3 + y^3}{x^2 + y^2} = 0$
6. Prove: If $F(x, y, z) = 0$ implicitly define a differentiable $z = z(x, y)$ then $\frac{\partial z}{\partial x} = -\frac{F_x}{F_z}$
7. Find the limits: $\lim_{(x,y) \rightarrow (0,0)} \frac{x + y}{x^2 + y}$
8. Show: $\frac{\partial w}{\partial u} + \frac{\partial w}{\partial v} = 0$ for $w = f(x, y), x = u - v$ and $y = v - u$
9. Show: If $w = f(x, y)$ and $x = r \cos \theta, y = r \sin \theta$ then $(\frac{\partial w}{\partial x})^2 + (\frac{\partial w}{\partial y})^2 = (\frac{\partial w}{\partial r})^2 + (\frac{1}{r^2})(\frac{\partial w}{\partial \theta})^2$
10. Find the area of the region inside $r = a(1 + \sin \theta)$ and outside $r = a \sin \theta$
11. Evaluate the integral by changing the order of integration:

$$\int_0^1 \int_{\sqrt{y}}^1 e^{-x^3} dx dy$$

12. Use cylindrical coordinate to find the mass of a solid Q of uniform density k , inside both $x^2 + y^2 + z^2 = a$ and $x^2 + (y - a/2)^2 = (a/2)^2$